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Tripotassium dibismuth(III) tris[arsenate(V)],  
 $K_3Bi_2(AsO_4)_3$ 

The title compound was prepared by a solid-state reaction at 1123 K. Its structure is closely related to that of alluaudite. The main structural feature is the presence of infinite chains of edge-sharing  $Bi_2O_{10}$  dimers, which are linked by  $AsO_4$  tetrahedra to form a framework enclosing two types of channels where  $K^+$  cations reside. The X1 site of the alluaudite structure is occupied by  $K^+$ , whereas the X2 site is empty.

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## Key indicators

Single-crystal X-ray study  
 $T = 293\text{ K}$   
 Mean  $\sigma(As-O) = 0.007\text{ \AA}$   
 $R$  factor = 0.026  
 $wR$  factor = 0.051  
 Data-to-parameter ratio = 12.7

For details of how these key indicators were automatically derived from the article, see <http://journals.iucr.org/e>.

## Comment

Phosphates such as  $M_3^I M_2^{III}(PO_4)_3$  ( $M^I = Li, Na, M^{III} = Cr, Fe, Sc$ ) have been extensively investigated. They are known to be fairly good ionic conductors, structurally related to Nasicon,  $Na_3Zr_2Si_2PO_{12}$ . In contrast, arsenates exhibit other structure types:  $Li_3Cr_2(AsO_4)_3$  has a garnet structure,  $Na_3Sc_2(AsO_4)_3$  is structurally related to  $\gamma$ - $Na_3Sc_2(PO_4)_3$  (hexagonal Nasicon-like structure), whereas the three compounds  $Li_3(Fe, In, Sc)_2(AsO_4)_3$  are structurally related to the monoclinic  $Fe_2(SO_4)_3$ . The investigation of Bi compounds has the added interest that structural modifications occur in the coordination polyhedra due to the non-bonding lone pair, leading to new structures. However, the effect of lone pairs has been studied by few authors. For these reasons, we have investigated the A–Bi–P–

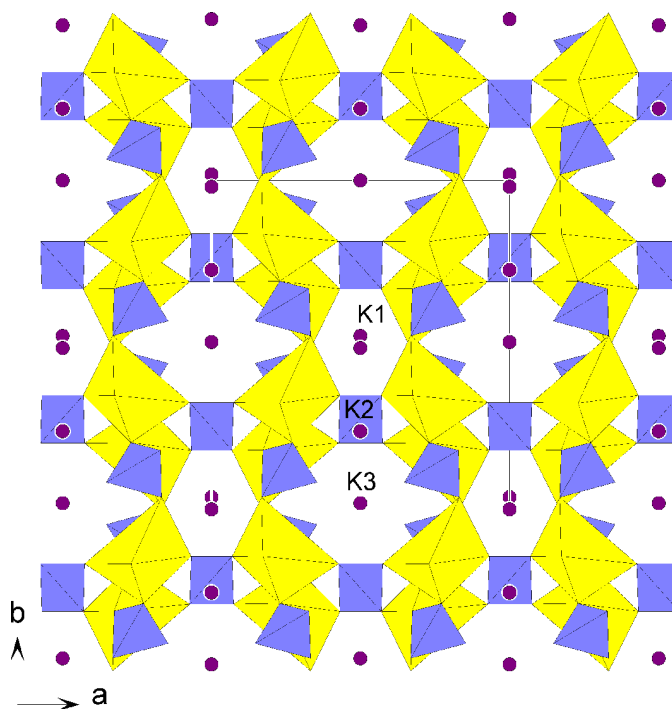
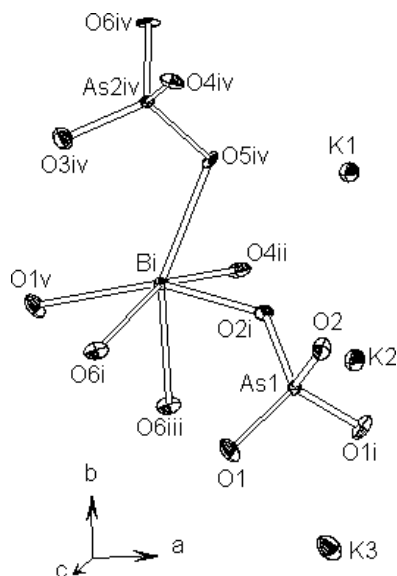


Figure 1

A projection of the structure of  $K_3Bi_2(AsO_4)_3$ , viewed along the  $c$  axis. Colour key:  $BiO_6$  polyhedra yellow and  $AsO_6$  polyhedra blue.



**Figure 2**

A view of a portion of the structure of  $K_3Bi_2(AsO_4)_3$ , with the atomic numbering scheme. Displacement ellipsoids are drawn at the 50% probability level.

O system ( $A$  = monovalent cation) and have previously reported the syntheses and crystal structures of  $Na_5Bi(P_2O_7)_2$  (Boughzala & Jouini, 1999),  $K_3Bi_2(PO_4)_3$  (Falah *et al.*, 2001) and  $Rb_6Bi_4(PO_4)_2(P_2O_7)_4$  (Falah *et al.*, 2003). In further investigations, we replaced P by As in order to find new alkali bismuth arsenate compounds in the  $A$ –Bi–As–O system ( $A$  being a monovalent cation). In this paper, we report the synthesis and X-ray structure determination of a new arsenate, *viz.*  $K_3Bi_2(AsO_4)_3$ .

The title compound has an alluaudite-like structure (Moore, 1971; Lii & Ye, 1997). In fact, there is a second known arsenate mineral with the alluaudite structure. The structure of the title compound is built up from  $BiO_6$  octahedra and  $AsO_4$  tetrahedra sharing corners to form a three-dimensional framework enclosing two types of channels where  $K^+$  ions reside (Fig. 1). The  $BiO_6$  octahedra appear to be more distorted than is usual for  $MO_6$  in the alluaudite structure, which is characteristic of the lone-pair effect. Bi is coordinated by three O atoms with short bonds [ $2.199$  (6) < Bi–O <  $2.296$  (7) Å] on one side and by three long bonds [ $2.505$  (6) < Bi–O <  $2.579$  (7) Å] on the other side (Fig. 2). This geometry is compatible with the stereoactivity of the bismuth lone pair, which points its orbital lobe between the longest Bi–O bonds. The Bi–O6 distance is characteristic of the triply bridging O atom O6, shared by  $As_2O_4$  tetrahedra and two  $BiO_6$  octahedra. The bond-valence sum using Brown's method (Brown & Altermatt, 1985), which gives 2.99, is in good agreement with the oxidation state of Bi. Comparison with the crystal structure of a natural alluaudite from the Buranga pegmatite of Central Africa (Moore, 1971; Yakubovich *et al.*, 1977) indicates that the X1 site at  $(\frac{1}{2}, 0, 0)$  is partly filled with  $Na^+$ ,  $Ca^{2+}$  and  $Mn^{2+}$ , whereas, in the title compound, the X1 site is fully occupied by K3. A new site shifted from the X1 site by  $\frac{1}{4}$  or  $-\frac{1}{4}$  in  $z$  at a general position near  $\frac{1}{2}, 0, z$  is fully occupied by K1. The X2 site is empty in

natural alluaudite and partly filled by cations smaller than  $K^+$  in other alluaudite-like structures, *viz.*  $Na_3In_2(AsO_4)_3$  (Khorari *et al.*, 1997) and  $NaCo_3(AsO_4)(HAsO_4)_2$  (Lii & Shih, 1994). In the title compound,  $K^+$  cannot be accommodated in this site and the X2 site remains empty. This is the reason why  $K^+$  has moved to the X1 site. The M1 site is occupied by K2 and the M2 site is filled by Bi, as observed in  $K_3Bi_2(PO_4)_3$  (Falah *et al.*, 2001). There are the two examples of the full occupancy of the X1 and M1 sites by  $K^+$  cations. K1, K2 and K3 ions are coordinated by ten, eight and six O atoms, respectively, with distances ranging from 2.681 (6) to 3.319 (7) Å, forming irregular coordination polyhedra. The bond-valence sums of the K–O bonds using the formula of Brown & Altermatt (1985) are 1.25, 1.28 and 1.11 for K1, K2 and K3, respectively. Thus, the high valence bond sums appear to compensate for the shortfall in the sums, 4.90 and 4.86, for As1 and As2.

## Experimental

The title compound can be prepared by solid-state reaction techniques. The synthesis procedure is as follows. Stoichiometric quantities of the appropriate reagents ( $K_2CO_3$ ,  $Bi_2O_3$  and  $NH_4H_2PO_4$ ) were intimately mixed and calcined in air at 623 K for 12 h in an alumina crucible. These ingredients were then heated to 1123 K for 40 d and finally cooled to room temperature in the furnace. The product was washed with boiling water. This led to the formation of parallelepiped-shaped colourless crystals of  $K_3Bi_2(AsO_4)_3$ .

### Crystal data

$K_3Bi_2(AsO_4)_3$   
 $M_r = 952.02$   
 Monoclinic,  $C2/c$   
 $a = 14.030$  (2) Å  
 $b = 13.773$  (2) Å  
 $c = 7.009$  (2) Å  
 $\beta = 114.71$  (2)°  
 $V = 1230.4$  (3) Å<sup>3</sup>  
 $Z = 4$

$D_x = 5.140$  Mg m<sup>-3</sup>  
 Mo  $K\alpha$  radiation  
 Cell parameters from 25 reflections  
 $\theta = 9.6$ – $14.9^\circ$   
 $\mu = 37.65$  mm<sup>-1</sup>  
 $T = 293$  (2) K  
 Parallelepiped, colourless  
 $0.11 \times 0.04 \times 0.04$  mm

### Data collection

Enraf–Nonius CAD-4 diffractometer  
 $\omega$ – $2\theta$  scans  
 Absorption correction:  $\psi$  scan (North *et al.*, 1968)  
 $T_{min} = 0.164$ ,  $T_{max} = 0.255$   
 1387 measured reflections  
 1203 independent reflections  
 1006 reflections with  $I > 2\sigma(I)$

$R_{int} = 0.021$   
 $\theta_{max} = 26.0^\circ$   
 $h = -17 \rightarrow 15$   
 $k = 0 \rightarrow 16$   
 $l = 0 \rightarrow 8$   
 2 standard reflections  
 frequency: 120 min  
 intensity decay: 2%

### Refinement

Refinement on  $F^2$   
 $R[F^2 > 2\sigma(F^2)] = 0.026$   
 $wR(F^2) = 0.051$   
 $S = 1.08$   
 1203 reflections  
 95 parameters

$w = 1/[\sigma^2(F_o^2) + (0.01P)^2]$   
 where  $P = (F_o^2 + 2F_c^2)/3$   
 $(\Delta/\sigma)_{max} = 0.001$   
 $\Delta\rho_{max} = 1.09$  e Å<sup>-3</sup>  
 $\Delta\rho_{min} = -1.22$  e Å<sup>-3</sup>  
 Extinction correction: SHELXL97  
 Extinction coefficient: 0.00050 (2)

**Table 1**

Selected geometric parameters (Å, °).

Bi—O2 <sup>i</sup>	2.199 (6)	K1—O2 <sup>vi</sup>	2.860 (7)
Bi—O4 <sup>ii</sup>	2.231 (6)	K1—O5	2.919 (6)
Bi—O6 <sup>iii</sup>	2.296 (7)	K1—O4	2.984 (7)
Bi—O5 <sup>iv</sup>	2.457 (7)	K1—O2 <sup>vii</sup>	3.319 (6)
Bi—O1 <sup>v</sup>	2.505 (6)	K2—O4	2.684 (6)
Bi—O6 <sup>i</sup>	2.579 (7)	K2—O1 <sup>viii</sup>	2.735 (7)
As2—O3	1.663 (6)	K2—O3 <sup>iii</sup>	2.865 (7)
As2—O5	1.694 (6)	K2—O2 <sup>vii</sup>	3.067 (7)
As2—O4	1.709 (6)	K3—O3 <sup>viii</sup>	2.681 (7)
As2—O6	1.717 (6)	K3—O3 <sup>iii</sup>	2.681 (7)
As1—O1	1.668 (7)	K3—O3 <sup>ix</sup>	2.757 (7)
As1—O2	1.716 (6)	K3—O1 <sup>x</sup>	2.854 (7)
K1—O5 <sup>vi</sup>	2.681 (6)		
O2 <sup>i</sup> —Bi—O4 <sup>ii</sup>	82.1 (2)	O1 <sup>v</sup> —Bi—O6 <sup>i</sup>	77.2 (2)
O2 <sup>i</sup> —Bi—O6 <sup>iii</sup>	80.7 (2)	O3—As2—O5	112.5 (3)
O4 <sup>ii</sup> —Bi—O6 <sup>iii</sup>	82.8 (2)	O3—As2—O4	108.4 (3)
O2 <sup>i</sup> —Bi—O5 <sup>iv</sup>	79.8 (2)	O5—As2—O4	108.3 (3)
O4 <sup>ii</sup> —Bi—O5 <sup>iv</sup>	79.9 (2)	O3—As2—O6	110.9 (3)
O6 <sup>iii</sup> —Bi—O5 <sup>iv</sup>	155.5 (2)	O5—As2—O6	107.0 (3)
O2 <sup>i</sup> —Bi—O1 <sup>v</sup>	155.3 (2)	O4—As2—O6	109.7 (3)
O4 <sup>ii</sup> —Bi—O1 <sup>v</sup>	108.1 (2)	O1 <sup>i</sup> —As1—O1	109.5 (5)
O6 <sup>iii</sup> —Bi—O1 <sup>v</sup>	78.5 (2)	O1 <sup>i</sup> —As1—O2	114.8 (3)
O5 <sup>iv</sup> —Bi—O1 <sup>v</sup>	123.5 (2)	O1—As1—O2	107.7 (3)
O2 <sup>i</sup> —Bi—O6 <sup>i</sup>	85.1 (2)	O1 <sup>i</sup> —As1—O2 <sup>i</sup>	107.7 (3)
O4 <sup>ii</sup> —Bi—O6 <sup>i</sup>	156.6 (2)	O1—As1—O2 <sup>i</sup>	114.8 (3)
O6 <sup>iii</sup> —Bi—O6 <sup>i</sup>	75.9 (2)	O2—As1—O2 <sup>i</sup>	102.3 (4)
O5 <sup>iv</sup> —Bi—O6 <sup>i</sup>	116.9 (2)		

Symmetry codes: (i)  $1-x, y, \frac{3}{2}-z$ ; (ii)  $1-x, y, \frac{1}{2}-z$ ; (iii)  $x-\frac{1}{2}, \frac{1}{2}-y, z-\frac{1}{2}$ ; (iv)  $1-x, 1-y, 1-z$ ; (v)  $\frac{1}{2}-x, \frac{1}{2}-y, 1-z$ ; (vi)  $x, 1-y, z-\frac{1}{2}$ ; (vii)  $x, y, z-1$ ; (viii)  $\frac{3}{2}-x, y-\frac{1}{2}, \frac{3}{2}-z$ ; (ix)  $\frac{3}{2}-x, \frac{1}{2}-y, 1-z$ ; (x)  $x, -y, z-\frac{1}{2}$ .

The maximum and minimum electron-density peaks are located 1.98 and 1.76 Å from K1 and O2, respectively.

Data collection: *CAD-4 EXPRESS* (Enraf–Nonius, 1994); cell refinement: *CAD-4 EXPRESS*; data reduction: *MolEN* (Fair, 1990); program(s) used to solve structure: *SHELXS86* (Sheldrick, 1990); program(s) used to refine structure: *SHELXL97* (Sheldrick, 1997); molecular graphics: *DIAMOND* (Brandenburg, 1998); software used to prepare material for publication: *SHELXL97*.

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